



# Justifications derived from inconsistent case bases using authoritativeness

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# AF-CBA

- Post hoc analysis
  - Model agnostic
  - Access to training data
  - Local explanations (justifications)
- 
- An explanation takes the form of an argument game for grounded semantics played between a proponent and opponent of an outcome, in which they take turns to attack the other's last argument.

# General idea

- Case base  $CB$  is the set of cases (precedents).
- A case  $c = (F(c), outcome(c))$  is a fact situation and an outcome (e.g.  $s$ ).
- A fact situation contains dimensions (features) with values ( $v(d, c) = x$ )
- Focus case: current case and its predicted outcome
  
- *A fortiori* assumption:  
The focus case should have the same outcome as a precedent case if the differences between these cases only serve to add further support for that same outcome.

## Comparing cases

- Given two fact situations  $F$  and  $F'$ ,  $F \leq_s F'$  iff  $v \leq_s v'$  for all  $(d, v) \in F$  and  $(d, v') \in F'$ .
- Given case base  $CB$  and fact situation  $F$ , deciding  $F$  for  $s$  is forced iff  $CB$  contains a case  $c = (F', s)$  such that  $F' \leq_s F$ .

- Any value assignment in the focus case that is not at least as favourable for the outcome as in the precedent is a relevant difference:

$$D(c, f) = \{(d, v) \in F(c) \mid v(d, c) \not\leq_s v(d, f)\}$$

- A best precedent to cite is one with the same outcome as the focus case and with the fewest relevant differences.

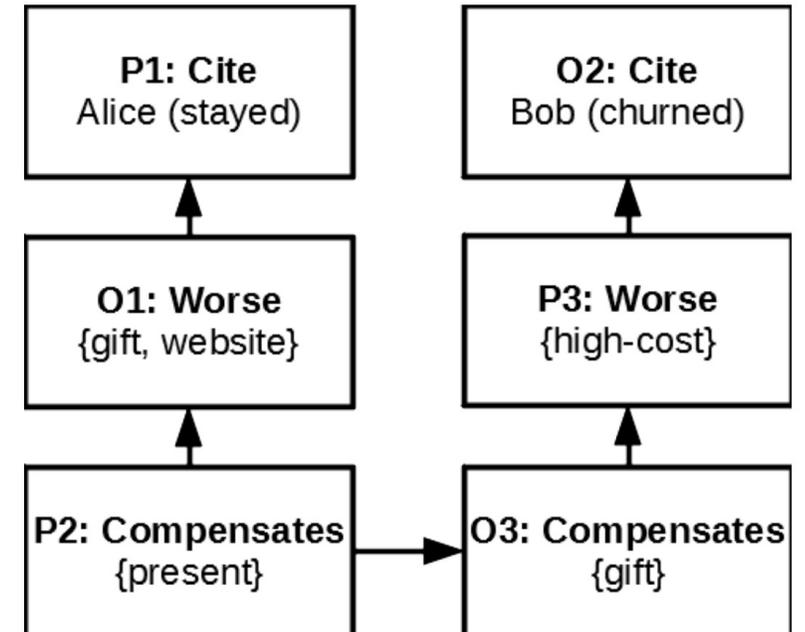
# Arguing over cases

- Proponent argues in favour of the predicted outcome, opponent argues against this by:
  - Citing a precedent  $c \in CB$
  - Distinguishing a cited precedent from focus case  $f \notin CB$  by:
    - *Worse*( $c, x$ ):  $f$  is on some dimensions  $x$  worse than  $c$  for *outcome*( $c$ ).
    - *Compensates*( $c, x, y$ ): the dimensions  $x$  on which  $f$  is not at least as good as  $c$  for *outcome*( $c$ ) are compensated by dimensions  $y$  on which  $f$  is better for *outcome*( $c$ ) than  $c$ .
    - *Transformed*( $c, c'$ ): initial citation can be transformed by the distinguishing moves into a case for which  $D(c, f) = \emptyset$  and which can therefore attack the counterexample.

# Example

Dimension	Name	Description
$d_1^\downarrow$	Gift	Whether the customer has received a gift from the provider
$d_2^\downarrow$	Present	Whether the customer was present during the last organised event
$d_3^\downarrow$	Website	The number of times the customer logged into their a profile
$d_4^\uparrow$	High cost	Whether the customer is in a high-cost category

Customer	$d_1^\downarrow$	$d_2^\downarrow$	$d_3^\downarrow$	$d_4^\uparrow$	Label (churn)
Alice	1	0	5	0	0
Bob	1	1	3	1	1
Charlie (focus)	0	1	3	0	?



# Inconsistency

- A case base  $CB$  is consistent iff it does not contain two cases with opposite outcomes such that  $F \leq_s F'$ .
- Case bases can be inconsistent because:
  - Annotators/decision makers can make mistakes or disagree.
  - Feature vectors can lack information to distinguish data.
- AF-CBA does not strictly require that the CB be consistent, but inconsistencies are often due to exceptional cases (with a surprising outcome) and these can be problematic for the explanation due to the focus case being forced for both outcomes.
- Explanations containing inconsistent forcings essentially explain that a decision cannot be justified without acknowledging the inconsistency of the CB, which weakens the value of those explanations.
- The larger the number of inconsistent forcings ( $N_{inc}$ ), the larger the number of explanations where this problem occurs.

# Authoritativeness

- In earlier work,  $N_{inc} = 0$  was achieved through case deletions. We would prefer to leave the case base (training data) intact and take the inconsistency of cases into account, preferably in a way which is intuitive.
- Previously: "Cases like this *always* receive outcome  $o$ "
- With this modification: "Cases like this *usually* receive outcome  $o$ "
- Cite the best precedent which has the highest value for authoritativeness  $\alpha(c)$ .

## Alternative expressions

$$n_a(c) = | \{c' \in CB \mid outcome(c') = outcome(c) \text{ and } D(c, c') = \emptyset\} |$$

The number of cases with the same outcome without any relevant differences.

$$\alpha(c) = \frac{n_a(c)}{n_a(c) + n_d(c)}$$

$$\alpha(c) = \frac{n_a(c)}{|CB|}$$

Both expressions capture some of the intuitive understanding of how authoritative a case is. We could therefore combine the two, e.g. as a product or harmonic mean.

This currently gives us four expressions for authoritativeness.

# Example

Customer	$d_1^\downarrow$	$d_2^\downarrow$	$d_3^\downarrow$	$d_4^\uparrow$	outcome
$c_1$	1	1	0	0	$s$
$c_2$	1	1	0	0	$s$
$c_3$	1	1	0	0	$s$
$c_4$	1	1	2	0	$s$
$c_5$	1	1	2	0	$s$
$c_6$	1	1	2	0	$\bar{s}$
$c_7$	1	1	15	0	$s$

$$\alpha(c_1) = 3/(3 + 0) = 1$$

or

$$\alpha(c_1) = 3/7 \approx 0.429$$

## Evaluation

	Base	Relative (1)	Absolute (2)	Product (3)	Harmonic ( $\beta = 1$ ) (4)
Admission	$\mu = 105.67$ $N_{inc} = 496$	$\mu = 112.1$ $N_{inc} = 0$	$\mu = 105.95$ $N_{inc} = 0$	$\mu = 106.0$ $N_{inc} = 0$	$\mu = 105.97$ $N_{inc} = 0$
Churn	$\mu = 82.15$ $N_{inc} = 38012$	$\mu = 148.81$ $N_{inc} = 2$	$\mu = 94.68$ $N_{inc} = 42$	$\mu = 94.76$ $N_{inc} = 0$	$\mu = 94.75$ $N_{inc} = 0$
Mushroom	$\mu = 70.25$ $N_{inc} = 620$	$\mu = 72.37$ $N_{inc} = 0$	$\mu = 84.66$ $N_{inc} = 0$	$\mu = 86.75$ $N_{inc} = 0$	$\mu = 84.83$ $N_{inc} = 0$

# Discussion and future work

- Why not use a simpler model instead?
  - There are problems for which the only satisfactory solutions are too opaque for practitioners.
- These metrics are only proxies, usability studies are required to study interpretability.
- Additional criteria for authoritativeness might turn out to be important, rendering our current expressions obsolete.
- Additional modifications of AF-CBA:
  - Other criteria for ranking precedents
  - Incorporating complex arguments
  - Accounting for highly dependent dimensions
  - Allow for dimensions with complex tendencies

# Conclusion

- Modification of AF-CBA so as to include the reality of inconsistent case bases, expressed through various alternative formulations.
- The authors would like to thank the anonymous reviewers for their feedback and suggestions.
- H. Prakken, R. Ratsma, A top-level model of case-based argumentation for explanation: formalisation and experiments, *Argument & Computation Preprint* (2021) 1–36. doi:10.3233/AAC-210009, publisher: IOS Press.



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