ALGORITHM XYZ. GEMM–Based Level 3 BLAS: Installation, Tuning and Use of the Model Implementations and the Performance Evaluation Benchmark

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Abstract

The GEMM-based level 3 BLAS model implementations, which are structured to effectively reduce data traffic in a memory hierarchy, and the performance evaluation benchmark, which is a tool for evaluating and comparing different implementations of the level 3 BLAS with the GEMM-based model implementations are presented in [5]. Here, the installation and tuning of the Fortran 77 model implementations, as well as the use and installation of the performance evaluation benchmark are described. All software come in all four data precisions and are designed to be easy to implement and use on different platforms. Each of the GEMM-based routines has a few system dependent parameters that specify internal block sizes, cache characteristics, and intersection points for alternative code sections.

1 Introduction

In [5] we described our portable and high-performance model implementations of the GEMM-based level 3 BLAS. Performance results for several different computer systems were also presented. Moreover, we described the GEMM-based level 3 benchmark, its purpose and design, and presented some benchmark results for different vendor-manufactured level 3 BLAS implementations.

The present contribution describes the installation and tuning of the GEMM-based model implementations in Section 2, and the use and installation of the performance evaluation benchmark in Section 3.

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All software come in all four data precisions with standard naming conventions and are available via the ACM Collected Algorithm services (and Netlib). The naming standard is that all routine names have a prefix-character (_), which is `s` for single precision real data, `d` for double precision real data, `c` for single precision complex data, and `z` for double precision complex data. This holds for all GEMM-based level 3 BLAS routines, auxilary routines, and all routines related to the GEMM-based benchmark. In the following we make illustrations only for the double precision real data case. The necessary changes for the other data types and precisions are obvious from the context.

2 Installation and Tuning of the GEMM-Based Level 3 BLAS

The purpose of this guide is to facilitate installation of the GEMM-based level 3 BLAS model implementations so that correct results are produced and high and uniform performance is achieved. The model implementations are primarily intended for single processor use, on machines with local or global caches, and for micro-processors with on-chip caches. They can also be parallelized using a parallelizing compiler, or linked with underlying parallel BLAS routines. Most of the machine characteristics of a target architecture are hidden and utilized in the underlying BLAS routines (_GEMM and some level 1 and level 2 BLAS routines).

2.1 Auxiliary routines

The implementation of _CLD is designed for a multi-way associative cache. The cache lines in a multi-way associative cache are divided among a number of partitions, each containing the same number of lines. The number of lines in a partition equals the associativity of the cache. For example, in a 4-way associative cache, each partition contains four cache lines, and up to four cache lines (with the same cache address determined by a mapping function) can be stored simultaneously in the cache. When data that is not in cache is requested, its cache line replaces one of the four lines currently stored (at the address assigned by the mapping function). The least recently used (LRU) line is a common cache replacement policy [2]. Other policies are based on some random choice for the line to be replaced.

The intersection points `_IP`x, where x is a number identifying a specific break point in a particular GEMM-based level 3 BLAS routine, are specified in _BIGP. These intersection points are used to determine which of two alternative code sections that will be the fastest, depending on the problem size. In the present implementation _BIGP looks at only one of the dimensions of a problem to determine the fastest code section.

It may be rewarding to modify _CLD for a machine with different cache policy, and _BIGP to involve both of the dimensions.

2.2 Machine-specific parameters

Each of the GEMM-based routines has system dependent parameters that specify internal block sizes, cache characteristics, and intersection points for alternative code sections. These values are given in PARAMETER statements, by the user or the system manager. A simple program _SGPM that facilitates tuning of the parameters is included in the GEMM-based package (see Section 2.3).

The internal blocking parameters r, c and rc used in the description of the model implementations (see Section 5 in [5]) have the names `RB`, `CB` and `RCB`, respectively, in the Fortran 77 routines. Local arrays of size `RCB` $\cdot$ `RCB` double precision words are allocated in each of the GEMM-based routines to hold general, symmetric, or triangular matrix blocks temporarily. Moreover, a local array of size `RB` $\times$ `CB` is allocated in each of _SYRK, _TRMM, and _TRSM, and a local array of size `CB` $\times$ `CB` in _TRMM and _TRSM.

_CLD has parameters specifying characteristics of the cache memory to determine which sizes of the leading dimension of a 2-dimensional array that should be considered critical:

`LNSZ` Size of a cache line in number of bytes.

`NPRT` Number of partitions in the cache memory.

`PRTSZ` The largest number of cache lines in each partition, that can be used exclusively to hold a local array containing a matrix block during the execution of a GEMM-based level 3 routine. The remaining cache lines are occupied by scalars, vectors and possibly program code, depending on the system characteristics.

`LOLIM` Leading dimensions smaller than or equal to `LOLIM` are not regarded as critical.

`_P` Size of the current precision word in number of bytes.

2.3 Guidelines for assigning values to the machine-specific parameters

The machine-specific parameters for the GEMM-based level 3 BLAS provide means for adjustment to some of the characteristics of a memory hierarchy. Considering the diversity of memory systems, the following guidelines for assigning values to the machine-specific parameters must be viewed as rules of thumb, rather than regulations.

- The block dimensions `RCB`, `RB`, and `CB`, should all be multiples of the number of double-precision words that fits in a cache line (`LNSZ/_P`).
- The three items that follow apply only to _SYRK, _TRMM, and _TRSM.
  - If the machine has vector registers, `RB` should equal the number of double-precision words that fits in a vector register.
  - A block of size `RB` $\times$ `CB` double-precision words should safely fit in the local cache memory, possibly together with scalars, two column vectors, of size `RB` and `CB`, and program code. Typically, `RB` $\cdot$ `CB` double-precision words correspond to 50–75% of the size of a local cache.

  - A block of size `RCB` $\times$ `RCB` double-precision words should safely fit in cache and occupy, for instance, 50–75% of a local cache.

  Notice that only one of the local blocks resides in cache at a given time.

- The following two items apply only to _SYMM and _SYR2K.
  - A local array of size `RCB` $\times$ `RCB` is allocated. The array does not need to fit in cache and should be fairly large but still reasonable in size. If vector registers are present, a good choice for `RCB` is the number of words that fit in a vector register, or possibly a multiple of that number.
  - In some cases, rows of length `CB` are referenced. `CB` cache lines should safely fit in the cache in order to become reused efficiently. `RCB` is an upper limit for `CB` in this case. If `CB` $>$ `RCB`, then `RCB` is used instead of `CB`.

- The intersection points `_IP`x used in _SYRK, _TRMM, and _TRSM, are assigned values in the routine _BIGP. If the the problem size is larger than or equal to `_IP`x, then _GEMV is invoked. The values for `_IP`x may differ between the alternative code sections depending on the values of `RCB`, `RB`, and `CB`. Values returned from _BIGP should effectively reflect the performance characteristics of the underlying level 2 BLAS routines. If _GEMV is carefully optimized, a proper value for `_IP`x may be found in the range 0–10 (0 corresponds to that all calls will be to _GEMV). Timing experiments with small matrix dimensions are recommended.

- Values for the parameters `LNSZ`, `NPRT`, and `_P` are obvious from the definitions (see Section 2.2).

- `PRTSZ` should be assigned the largest number of cache lines that, in each partition, can be used to hold a local array containing a matrix block. If the cache is shared for program instructions and data, a suitable value for `PRTSZ` is the total number of cache lines in a partition minus one, or two, leaving one or two cache lines in each partition for vectors, scalars, and program code.

- `LOLIM` is a lower limit for the size of the leading dimension that may be considered critical. We use `LOLIM` = max(`RCB`, `RB`), where `RCB` and `RB` are the block dimensions given for _SYRK, _TRMM, and _TRSM.

The parameter values for internal block sizes and intersection points are adjusted separately for each routine. It can be rewarding to experiment with a range of different values for these parameters in order to optimize the performance.

If you are unable to make the function _CLD safely predict which leading dimensions that will cause substantial performance degradation, you may consider modifying _CLD so that the value `.TRUE.` is always returned for values greater than `LOLIM`. In this case, all leading dimensions greater than `LOLIM` are regarded as critical. The risk of severe performance degradation for the GEMM-based routines becomes significantly reduced, at the small expense of copying matrix blocks to local arrays a few more times.

The GEMM-based level 3 BLAS benchmark can be used to fine-tune the machine-specific parameters for high performance. Another useful timing program is distributed with the original level 3 BLAS [3, 4]. For example, the double precision real version can be obtained by sending the E-mail message ‘send dblas3time from blas’ to netlib@ornl.gov.

2.4 Sample values for the machine-specific parameters

The values for the machine-specific parameters presented here are the best values we have found experimentally, but there is no guarantee that they are optimal and should merely be viewed as starting-values for further refinement. They have been used during the development of the GEMM-based level 3 BLAS model implementations and for benchmarking on several different computer systems.

The program _SGPM modifies the GEMM-based level 3 BLAS source files replacing lines containing old PARAMETER statements for machine-specific parameters, with lines containing new PARAMETER statements given in the input file. The user (or system manager) can conveniently assign new values to the PARAMETER statements in the input file, and then run _SGPM to distribute the values among the GEMM-based routines. The files `dsgpm.f` and `dgpm.in` contain the program DSGPM and an example input file, respectively. An input file to _SGPM consists of three different types of lines, apart from empty lines.

- Comment lines starting with the character ‘`*`’.
- Lines containing single filenames for GEMM-based source files.
- Lines containing PARAMETER statements that replace the corresponding lines in the GEMM-based routines.

A line containing a filename is followed by lines containing the new PARAMETER statements for the particular file.

Input file for IBM RS/6000 530H is displayed in Figure 1. The following machine characteristics are used to determine values for the parameters. This machine has separate caches for data and instructions, where the size of the data cache is 64 Kbyte with 128 bytes cache lines. The cache scheme is 4-way associative (mapping) and the size of a double word is 8 bytes.

In tables 1, 2 and 3 we show sample values of the machine-specific parameters for some different architectures. Notably, the best values on the intersection points in Table 2 are all the same for the architectures we have considered, except for Alliant FX/2800 for which we used all values equal to 3. Table 3 also displays some cache memory characteristics, namely the associativity of the cache, cache size (in Kbytes) and cache line size (in bytes). Notice that the SGI machines have a direct mapped cache and that some of the machines have a separate data cache (D in the table), while others have a common instruction and data cache (C in the table).

2.5 Installing the programs

This section describes how to install the GEMM-based level 3 BLAS model implementations on a Unix-based system. A `makefile` is included in the GEMM-based package to facilitate the installation.

Figure 1: Input file for IBM RS/6000 530H.

```
dsymm.f
      PARAMETER        ( RCB = 128, CB = 64 )
dsyr2k.f
      PARAMETER        ( RCB = 128, CB = 64 )
dsyrk.f
      PARAMETER        ( RCB = 64, RB = 64, CB = 64 )
dtrmm.f
      PARAMETER        ( RCB = 64, RB = 64, CB = 64 )
dtrsm.f
      PARAMETER        ( RCB = 64, RB = 64, CB = 64 )
dbigp.f
      PARAMETER        ( DIP41 = 4, DIP42 = 3,
     $                   DIP81 = 4, DIP82 = 3, DIP83 = 4,
     $                   DIP91 = 4, DIP92 = 3, DIP93 = 4 )
dcld.f
      PARAMETER        ( LNSZ = 128, NPRT = 128, PRTSZ = 3,
     $                   LOLIM = 128, DP = 8 )
```

The machine-specific parameters come with default values. These values need to be optimized for different target machines according to the guidelines in Section 2.3. Some experiments with different values may result in a remarkable increase in performance, and is therefore recommended.

The program _SGPM together with an input file can be used to assign values to the machine-specific parameters. Compile and link the program _SGPM:

```
% make dsgpm
```

Create a copy, `newdgpm.in`, of the enclosed input file `dgpm.in`. Assign new values to the machine-specific parameters in `newdgpm.in` (see the guidelines in Section 2.3 and the examples in Section 2.4). Run the program which rewrites the GEMM-based routines with the new parameter values given in `newdgpm.in`:

```
% dsgpm < newdgpm.in
```

Decide whether you wish to create a complete level 3 BLAS library, including the underlying BLAS routines, or a library with only the GEMM-based level 3 BLAS routines, which need to be linked with the underlying BLAS at a later stage, when an executable program is created.

For a complete library, assign the underlying BLAS (paths to routines, or to a library, containing the underlying BLAS) to the variable LIB12B in `makefile`. If you wish, you may specify a separate underlying _GEMM routine to the variable xGEMM in `makefile`. For a library containing only the GEMM-based routines, do not specify any routines or libraries. You may also specify compiler flags in `makefile`. Create a GEMM-based level 3 BLAS library:

```
% make libgbl3b
```

Table 1: Sample values for internal blocking parameters.

Computer system:		DSYMM	DSYRK	DSYR2K	DTRMM	DTRSM
Alliant FX/2816	RB	-	32	-	32	32
	CB	32	32	32	32	32
	RCB	128	32	128	32	32
IBM 3090J-VF	RB	-	256	-	256	256
	CB	96	96	96	96	96
	RCB	256	144	256	144	144
IBM RS6000 250	RB	-	56	-	56	56
	CB	56	56	56	56	56
	RCB	128	56	128	56	56
IBM RS6000 530H	RB	-	64	-	64	64
	CB	64	64	64	64	64
	RCB	128	64	128	64	64
IBM SP2 thin	RB	-	96	-	96	96
	CB	96	96	96	96	96
	RCB	256	96	256	96	96
IBM SP2 wide	RB	-	144	-	144	144
	CB	144	144	144	144	144
	RCB	256	144	256	144	144
Intel Paragon	RB	-	40	-	40	40
	CB	40	40	40	40	40
	RCB	128	40	128	40	40
Parsytec(80Mhz)	RB	-	48	-	48	48
	CB	48	48	48	48	48
	RCB	144	48	144	48	48
SGI Indy R4000	RB	-	32	-	32	32
	CB	24	24	24	24	24
	RCB	128	24	128	24	24
SGI Indy R4400	RB	-	48	-	48	48
	CB	32	32	32	32	32
	RCB	128	32	128	32	32

Table 2: Sample values for intersection points used in DBIGP.

Computer system:	DIP41	DIP42	DIP81	DIP82	DIP83	DIP91	DIP92	DIP93
IBM SP2 thin	4	3	4	3	4	4	3	4

If everything worked out well, a library named `libgbl3b.a` has been created in the directory above the current directory.

Table 3: Cache caharacteristics and sample values for parameters used in DCLD.

Computer system:	Associ-ativity	Cache size Kbytes	Line size Bytes	LNSZ	NPRT	PRTSZ	LOLIM	DP
Alliant FX/2816	2-way	8 (D)	32	128	128	2	32	8
IBM 3090J-VF	4-way	256 (C)	128	128	512	3	128	8
IBM RS6000 250	8-way	32 (C)	64	64	64	6	64	8
IBM RS6000 530H	4-way	64 (D)	128	128	128	3	128	8
IBM SP2 thin	4-way	128 (D)	128	128	256	3	128	8
IBM SP2 wide	4-way	256 (D)	256	256	256	3	256	8
Intel Paragon-XP	2-way	16 (D)	32	32	512	2	40	8
Parsytec(80MHz)	8-way	32 (C)	64	64	64	6	64	8
SGI Indy R4000	direct	8 (D)	32(64)	32	128	2	32	8
SGI Indy R4400	direct	16 (D)	32(64)	32	256	2	32	8

2.6 Verification of the correctness of the installed programs

Be sure to verify the correctness of the compiled routines thoroughly, before production use. Do not trust the underlying BLAS, or the compiler used, especially if compiler options for code optimization, inlining, etc., were used. We recommend the test program DBLAT3 for verification of double-precision level 3 BLAS [3, 4]. Apart from the block sizes you have selected for best performance, make some tests with small block dimensions. For example, different combinations of the values 3, 4, and 7 for the parameters `RCB`, `RB`, and `CB`, respectively. Matrix dimensions in the range 0–60 should be satisfactory. Include at least one test with dimensions larger than 30, to make sure that the block partitioning works correctly. For the scalars `alpha` and `beta` use, for instance, the values 0.0, 1.0, −1.0, −0.8, and 1.2.

3 Performance Evaluation Benchmark

The purpose of this guide is to facilitate the use and installation of the GEMM-based level 3 benchmark [5]. In brief, we describe the input file, benchmark results and how to install and use the benchmark.

To avoid extensive cross referencing between the two papers we will repeat some information from Section 7 in [5], for example, the output optionally computed by the benchmark:

A Tables, showing measured performance results in Mflops, and comparisons between different routines calculated as the performance result of one GEMM-based level 3 BLAS routine divided by the performance result of the corresponding user-specified level 3 routine.

B A collected "mean value" statistic, calculated from the performance results of the separate user-specified level 3 routines for the specified problem configurations.

3.1 The input file

The user supplies an input file for the benchmark specifying tests to be made and results to be presented. The following parameters need to be specified in the input file.

`LBL` An arbitrary label which identifies the test to be performed (max 50 characters). The label is printed together with the output results A and B.

`TAB` One or more numbers specifying tests to be made and results to be presented.

`RUNS` All results presented are based on the fastest of `RUNS` executions for each problem configuration.

At least one of the numbers 1–6 need to be specified for the parameter `TAB`. The numbers are interpreted as follows.

1. The collected benchmark result.
2. Performance of the built-in GEMM-based level 3 BLAS library in Mflops.
3. Performance of the user-specified level 3 BLAS library in Mflops.
4. Performance of the user-specified _GEMM routine in Mflops. Problem configurations for _GEMM are chosen to "correspond" to those in 2 and 3 for timing purposes (see Section 3.2).
5. GEMM-efficiency of the user-specified level 3 routines.
6. GEMM-ratio.

Both GEMM-efficiency and GEMM-ratio are defined in [5] (Section 7).
The input parameters for the level 3 BLAS routines are specified as follows.

`side` Characters. `L`(eft) and/or `R`(ight).

`uplo` Characters. `U`(pper) and/or `L`(ower) triangular part.

`trans` Characters. `N`(o transpose) and/or `T`(ranspose).

`diag` Characters. `N`(o unit) and/or `U`(nit) triangular.

`dim1` Integer values for the first of the two dimensions.

`dim2` Integer values for the second of the two dimensions.

`lda` Integer values for leading dimension of the matrices.

See [3, 4] for further explanations of the input parameters `side`, `uplo`, `trans`, and `diag`. The parameters `dim1` and `dim2` are used to specify the first and second dimensions in the calling sequence of the level 3 BLAS routines, respectively. The values for `dim1` and `dim2` come in pairs. `lda` (= `ldb` = `ldc`) specifies the leading dimension of the matrices A, B, and C in calls to the level 3 BLAS routines.

Specify for each routine whether it should be timed or not. Put `T` after the routine name if the routine should be timed, otherwise `F`. An example of an input file is given in the file `example.in`, which can be used as a template for user-constructed tests (see Figure 2).

Figure 2: Sample input file for GEMM-based benchmark.

```
LBL    Example 1, double precision.
***  Benchmark results to be presented  ***
TAB    1 2 3 4 5 6
***  RUNS executions of each problem configuration  ***
RUNS   2
***  Values of input parameters for the level 3 BLAS routines  ***
SIDE   L R
UPLO   U L
TRANS  N T
DIAG   N
DIM1    32  64 256 256
DIM2   256 256  32  64
LDA    256
***  Routines to be timed  ***
DSYMM  T
DSYRK  T
DSYR2K T
DTRMM  T
DTRSM  T
```

3.2 Benchmark results

The output from the benchmark optionally includes a "collected mean value" statistic of the user-specified level 3 routines, and tables showing detailed performance results and comparisons between the user-specified and the built-in GEMM-based level 3 BLAS routines (see Section 7 in [5]). Problem configurations, routines to be timed, and results to be presented are selected according to specifications in the input file.

3.2.1 The table results

The performance of the level 3 routines to be benchmarked are compared with the performance of _GEMM with the input parameters given in Table 4. We use `alpha` = 0.9, `beta` = 1.1, and `lda` = `ldb` = `ldc`. Notice the parameters of _GEMM that are not displayed are equal to the parameters of the GEMM-based routine it is compared with.

The number of floating point operations (flops) performed by a level 3 BLAS routine is divided by the execution time in seconds, times 10^6, to obtain the performance in Mflops. The number of flops of the level 3 BLAS operations are dispayed in Table 5.

3.2.2 The collected benchmark result

The purpose of the collected benchmark result is to expose the capacity of the target machine for level 3 kernels and to show how well the routines utilize the machine. Furthermore, the collected result is intended to be easy to compare between different computer systems.

Table 4: Input parameters for _GEMM.

GEMM-based routines			Input parameters for _GEMM								
routine	**side**	**trans**	**transa**	**transb**	m	n	k	A	B	C	**beta**
_SYMM	'L'		'N'	'N'	m	n	m	A	B	C	1.1
	'R'		'N'	'N'	m	n	n	B	A	C	1.1
_SYRK		'N'	'N'	'T'	n	n	k	A	A	C	1.1
		'T'	'T'	'N'	n	n	k	A	A	C	1.1
_SYR2K		'N'	'N'	'T'	n	n	k	A	B	C	1.1
		'T'	'T'	'N'	n	n	k	A	B	C	1.1
_TRMM,	'L'		trans	'N'	m	n	m	A	B	C	1.0
_TRSM	'R'		'N'	trans	m	n	n	B	A	C	1.0

Table 5: Number of flops for level 3 BLAS.

GEMM-based routines					
			nops	:	number of operations for a level 3 BLAS problem
routine	**side**	**diag**	gops	:	number of operations for the corresponding _GEMM problem
_SYMM	'L'		nops	=	$(2m+1)mn + \min(mn, m(m+1)/2)$
			gops	=	$(2m+1)mn + \min(mn, mm)$
	'R'		nops	=	$(2n+1)mn + min(mn, n(n+1)/2)$
			gops	=	$(2n+1)mn + min(mn, nn)$
_SYRK			nops	=	$(2k+1)(n(n+1)/2) + min(nk, n(n+1)/2)$
			gops	=	$(2k+1)nn + \min(nk, nn)$
_SYR2K			nops	=	$(4k+1)(n(n+1)/2) + \min(2nk, n(n+1))$
			gops	=	$(2k+1)nn + \min(nk, nn)$
_TRMM,	'L'	'N'	nops	=	$mmn + \min(mn, m(m+1)/2)$
_TRSM	'L'	'U'	nops	=	$mmn - mn + \min(mn, m(m+1)/2)$
	'L'		gops	=	$(2m-1)mn + \min(mn, mm)$
	'R'	'N'	nops	=	$mnn + \min(mn, n(n+1)/2)$
	'R'	'U'	nops	=	$mnn - mn + \min(mn, n(n+1)/2)$
	'R'		gops	=	$(2n-1)mn + \min(mn, nn)$

We propose two standard test suits for the collected benchmark result, _MARK01 and _MARK02 (see the files `dmark01.in` and `dmark02.in`). These tests are designed to show performance of the user-specified level 3 library for problem sizes that often are likely to be requested by a calling routine. For example, LAPACK implements blocked algorithms which are based on calls (with varying problem configurations, e.g., size and operation) to the level 3 BLAS [1].

The problems in the two tests are similar. However, some of the matrix dimensions are larger in _MARK02 than in _MARK01. This corresponds to larger matrix blocks in the calling routine. The tests are expected to match various target machines differently.

Since performance results depend strongly on sizes of different storage units in the memory hierarchy, we propose two standard tests instead of one.

3.3 The built-in GEMM-Based level 3 BLAS

The GEMM-based level 3 BLAS model implementations are included in the benchmark [5] and are used in the evaluation of another set of implementations. In order to keep the benchmark general, and make it possible to test variants of our model implementations, we have renamed the level 3 routines in the GEMM-based benchmark.

The new names are _GB02 (for _SYMM), _GB03 (for _HEMM), _GB04 (for _SYRK), _GB05 (for _HERK), _GB06 (for _SYR2K), _GB07 (for _HER2K), _GB08 (for _TRMM), _GB09 (for _TRSM), _GB90 (for _BIGP), and finally _GB91 (for _CLD). The reason for renaming the two new auxilary routines is that it makes it possible to compare the same GEMM-based model implementations, but with two different sets of auxilary routines.

3.4 Installing the benchmark program

All routines are written in Fortran 77 for portability. No changes to the code should be necessary in order to run the programs correctly on different target machines. Indeed, we strongly recommend the user to avoid changes, except for the machine-specific parameters and for `unit` numbers for input and output communication. This will ensure that performance results from different target machines are comparable. `unit` numbers are set in the main program _GBTIM and the machine-specific parameters exist only in the built-in GEMM-based level 3 BLAS routines.

The benchmark program consists of the following routines apart from the built-in GEMM-based level 3 BLAS routines:

_GBTIM is the main program which reads the input file and calls the routines described below.

_GBT01 times the user-specified _GEMM routine.

_GBT02 times the built-in GEMM-based level 3 BLAS routines and the user-specified level 3 BLAS routines except _GEMM.

_GBTP1 calculates and prints the collected benchmark result B.

_GBTP2 calculates and prints the table results A.

The following is a description of how to install the GEMM-based level 3 BLAS benchmark on machines with Unix-based operating systems. A `makefile` is enclosed to facilitate the installation. The user-specified parameters of the built-in GEMM-based level 3 BLAS routines come with default values, which might need to be optimized for the target machine (see sections 2.3 and 2.4).

The program _SBPM assigns values to the machine-specific parameters, and corresponds to the program _SGPM for the GEMM-based level 3 BLAS model implementations. Input files for _SGPM may also be used with _SBPM. To compile and link _SBPM give the command:

```
% make dsbpm
```

Run _SBPM which updates the built-in GEMM-based level 3 BLAS routines with the new parameters given in the input file, `newdgpm.in`:

```
% dsbpm < newdgpm.in
```

The benchmark program calls a function SECOND (or DSECND in double precision) with no arguments. This function is assumed to return the CPU time in seconds from some fixed starting time. Create this function if it does not already exist on your system. The enclosed Fortran 77 function in the file `dsecnd.f` can be used as a template. This routine is based on calls to the timing function etime under Unix.

Specify the level 3 BLAS library to be evaluated and compiler flags in `makefile`. You may change the `unit` numbers for I/O communication `nin`, `nout`, and `nerr` in the main program _GBTIM, if necessary. Create the executable benchmark program by giving the command:

```
% make dgbtim
```

If everything worked out well, you will now have a useful performance evaluation tool for level 3 BLAS kernels.

3.5 Executing the benchmark program

The GEMM-based level 3 BLAS benchmark can be used in different ways to evaluate performance of level 3 BLAS routines. It is possible to obtain one, or both, of the output results A and B described in previous sections. The user controls which tests to be made and which results to be presented through specifications in the input file.

The following Unix command runs the benchmark program with the input file `example.in` and writes the result to the output file `example.out`:

```
% dgbtim < example.in > example.out
```

Notice that this benchmark may be quite time consuming to run. Obviously, the "size" of the test, specified in the input file, is decisive for the execution time. Moreover, the performance of the target machine and of the different level 3 BLAS libraries also affect the total execution time.

3.6 Collecting benchmark results

We encourage users to help us collect performance results from different target machines. Please, send results obtained with the proposed standard tests _MARK01 and _MARK02 to the second author at E-mail address per.ling@cs.umu.se. Contributors that provide interesting results from the GEMM-based level 3 BLAS benchmark will be acknowledged in a future collection of bechmark results. We also encourage users to send comments on the model implementations and benchmark to any of the authors.

In order to be able to interpret the results we also need to have as much as possible of the following system characteristics specified:

- Machine: name and version, number of processors, sizes of cache(s) and main memory, etc.
- Operating system: name, version, and release.
- Fortran compiler: name, version, release, and options used.
- User-specified underlying BLAS: name of library, version, and release.
- Machine configuration used in the benchmark.
- Precision tested (S, D, Z or C), double precision: x-bit words.
- Timing function: describe the implementation of SECOND or DSECND. Specify which local timing function it is based on (e.g., etime, dclock, mclock), and which time it measures (e.g., real time, CPU-time, user-time) and to which resolution.

If the GEMM-based level 3 BLAS model implementations are the user-specified routines in the tests, please enclose values for the machine-specific parameters and describe the underlying BLAS implementations (_GEMM, level 1 and level 2 BLAS). If more than one processor are used, please explain how the parallelism is invoked. For example, whether the GEMM-based routines are automatically parallelized by the compiler and/or you are using parallel versions of the underlying BLAS routines.

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