

ESLLI 2016 course

**Foundations of Graph Transformation and Graph Grammars**

Lecture 5: *Further Topics, Implementations, and Literature*

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# Introduction



## Yesterday:

- We had a look at (counting) monadic second-order logic on graphs.
- Two variants, depending on whether edges can be quantified over.
- These are closely connected to context-free graph languages.
- MSO properties can be checked in fixed-parameter linear time.

## Further topics touched upon today:

- Term graph rewriting
- DAG automata
- Implementations
- Books and Surveys

# Term Graph Rewriting



# Term Rewriting and Sharing

Term rewriting is closely related to functional programming languages.

Example: the Fibonacci function

Haskell notation	Term rewrite rule
$fib\ 0 = 0$	$fib(0) \rightarrow 0$
$fib\ (s\ 0) = s\ 0$	$fib(s(0)) \rightarrow s(0)$
$fib\ (s\ (s\ x)) = (fib\ (s\ x)) + (fib\ x)$	$fib(s(s(x))) \rightarrow fib(x) + fib(s(x))$
$x + 0 = x$	$x + 0 \rightarrow x$
$x + (s\ y) = s\ (x + y)$	$x + s(y) \rightarrow s(x + y)$

Evaluation is straightforward but inefficient:

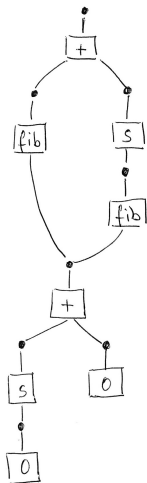
- Large terms with many identical subterms may occur.
- This is a waste of time and memory space.
- So, why not use sharing?



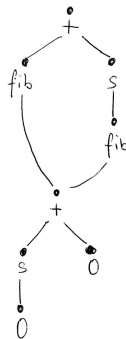
# Graphs Representing Trees

To make use of sharing, we can represent terms as (hyper)graphs and implement term rewriting by graph transformation.

Example:  $fib(s(0) + 0) + s(fib(s(0), 0))$

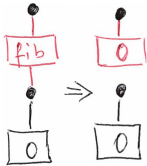


Simplified drawing:

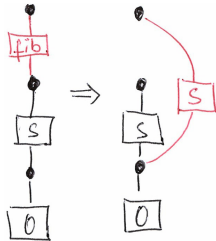


# Example: Term Rewriting by Graph Transformation

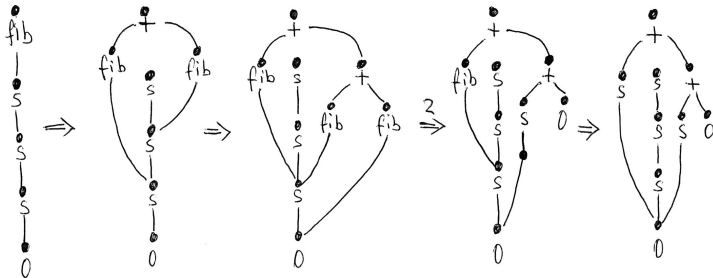
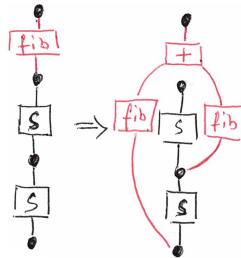
$$fib(0) \rightarrow 0$$



$$fib(s(0)) \rightarrow s(0)$$

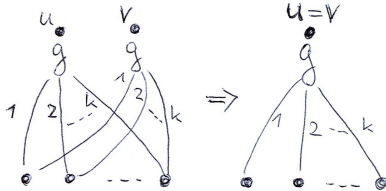


$$fib(s(s(x))) \rightarrow fib(x) + fib(s(x))$$

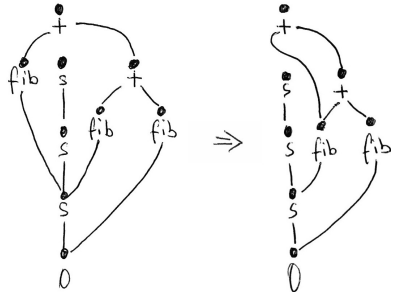


# Collapsing and Garbage

Collapsing nodes that represent identical subtrees by **merging rules** increases efficiency (but removes degrees of freedom):



collapsing rule



collapsing step

On the right we also observe the phenomenon of **garbage**.

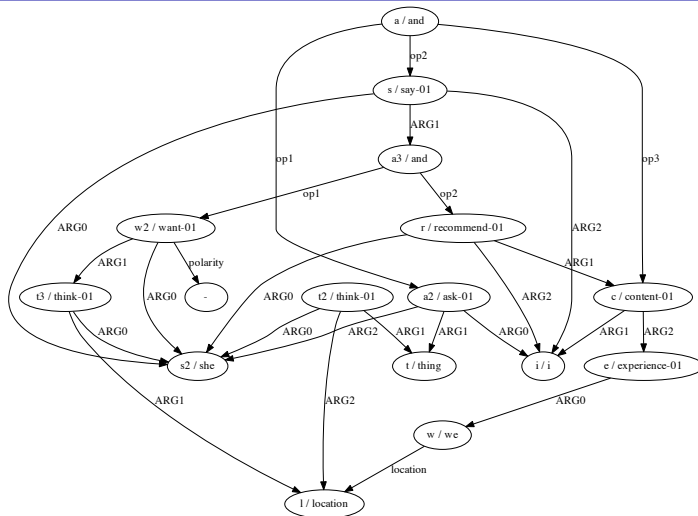
# DAG Automata



# Automata on Directed Acyclic Graphs?

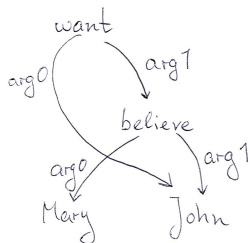
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- There is no generally accepted notion of **graph automata**.
- The difficulty is that there is **no sense of direction**.
- But in many areas **directed acyclic graphs** (DAGs) suffice.
- Term graphs and, in NLP, **meaning representations** are examples.
- Various types of DAG automata have been proposed in the literature.
- For NLP, **good algorithmic properties** are preferable over power.
- This calls for a **simple** notion.
- The possibility to **add weights** would enhance their usefulness.
- **Tree automata** should be a special case.

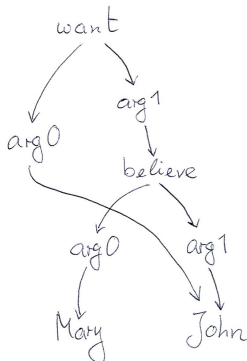


Abstract Meaning Representation (AMR) of “I asked her what she thought about where we’d be and she said she doesn’t want to think about that, and that I should be happy about the experiences we’ve had (which I am).”

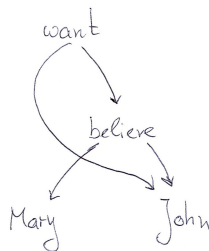
John wants Mary to believe him in slightly changing representations



use **edge labels**



encode using  
**intermediate nodes**

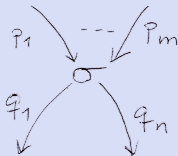


use **ordered** DAGs

# A Simple, Ranked Type of DAG Automata

## DAG automaton

- 1 A **run** is an assignment of **states** to edges.
- 2 **Rules** are of the form  $p_1 \cdots p_m \xrightarrow{\sigma} q_1 \cdots q_n$ .



- 3 A DAG is **accepted** if there is a run which is consistent with the rules at each node.

## Notes

- 1 **Tree automata** are a special case.
- 2 No **initial** and **final states** are required.
- 3 DAGs may be viewed as **ordered** or **unordered**.

Weighted DAG automata assign a **weight**, say in  $\mathbb{R}$ , to each DAG:

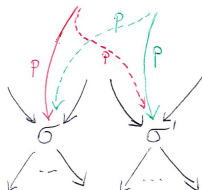
- Each rule gets a weight in  $\mathbb{R}$ .
- Weight 0 means that the rule “does not exist”.
- The weight of a run is the **product** of its rules’ weights.
- The weight of a DAG is the **sum** of the weight of all its runs.

## Notes

- ①  $\langle \mathbb{R}, +, \cdot \rangle$  may be replaced by any commutative semiring.
- ② The Boolean semiring corresponds to the unweighted case.
- ③ Again, weighted tree automata are a special case.

# Invariance under Edge Swapping

In a run, targets of edges with the same state can be swapped:



**Results** whose proofs exploit edge swaps:

- 1 Two types of **pumping lemmas**.
- 2 The **path language** of a regular DAG language is regular.
- 3 If  $L$  is finite, it is regular iff no  $D \in L$  contains an undirected cycle.
- 4 **Unfolding** turns regular DAG languages into regular tree languages.
- 5 **Emptiness** and **finiteness** are decidable in polynomial time.
- 6 **Deterministic DAG automata** can be minimized uniquely, and thus checked for language equivalence, in polynomial time.

### More results:

- ① The class of HR languages is closed under **intersection with regular DAG languages** (by a Bar-Hillel construction).
- ② Even **non-uniform membership** is, once again, **NP-complete**.
- ③ But **bounded treewidth** yields a polynomial algorithm.
- ④ All of this can be extended to DAG automata on DAGs with **unbounded in- and out-degree**. In these automata, heads and tails of rules are given by regular expressions.

# Implementations and Literature



# The Attributed Graph Grammar System

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AGG, TU Berlin, developed since the beginning of the 1990s; latest release so far is from 2015.

- Algebraic graph transformation (single-pushout, see 1st lecture)
- Extended by positive and negative application conditions
- Nodes and edges can have attributes which are Java objects
- Comes with a graphical user interface, but you can also use the transformation engine alone for building your own system

URL: <http://www.user.tu-berlin.de/o.runge/agg/>



# GGraphs for Object-Oriented VErification

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Groove, University of Twente, developed since 2003 (?), latest release just a few weeks old.

- Algebraic graph transformation (single-pushout, see 1st lecture)
- Intended as a verification tool that explores the state space generated by the rules
- Three separately available subsystems: interactive graphical user interface, graph transformation engine, model checker for verifying linear temporal logic formulae

URL: <http://groove.cs.utwente.nl>



GrGen.NET, University of Karlsruhe, developed since 2003, latest release from Feb 2016.

- Algebraic graph transformation (single-pushout, see 1st lecture) with some additions and ordinary programming constructs
- Extremely efficient rule application
- Comes with a graphical user interface for rapid prototyping, but the libraries can be used without

URL: <http://www.info.uni-karlsruhe.de/software/grgen>

# The Diagram Editor Generator

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[DiaGen/DiaMeta](#), UniBw Munich, developed since a long time back, latest release from 2012(?)

- Diagram editor generator that includes a hyperedge-replacement engine and parser used for specifying/checking the logical structure of diagrams
- The HR engine/parser can be used as a backend for other purposes
- Parsing is **fault tolerant** to handle inputs in a meaningful way even if they are only partially correct

URL: <https://www.unibw.de/inf2/DiaGen>



**Bolinas**, USC/ISI, developed since 2012(?), latest release from 2013

- Python package for synchronous hyperedge-replacement grammars with weights
- Algorithms for rule extraction from examples, training, parsing, k-best derivation.

URL: <http://www.isi.edu/licensed-sw/bolinas>



Alto, University of Potsdam, latest release from just a few weeks ago.

- Not a dedicated graph transformation system, but **interpreted regular tree grammars**
- One of the available algebras is Courcelle's HR algebra  
⇒ yields an implementation of (synchronous) HR grammars
- Includes parsing and other related algorithms
- Claims to be “the fastest published HRG parser in the world”

URL: <https://bitbucket.org/tclup/alto>

- Ehrig, Ermel, Golas, Hermann: *Graph and Model Transformation – General Framework and Applications*. Springer 2015.
- Courcelle, Engelfriet: *Graph Structure and Monadic Second-Order Logic – A Language-Theoretic Approach*. Cambridge University Press 2012.
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- Joost Engelfriet: *Context-Free Graph Grammars*. In Handbook of Formal Languages, Vol 3: Beyond Words. Springer 1997
- Annegret Habel: *Hyperedge Replacement: Grammars and Languages*. LNCS 643, Springer 1992