

# Hierarchically Blocked Algorithms and Optimized Kernels for Dense Matrix Computations on Memory-Tiered High-Performance Computing Systems

## Publications 2002–2009 within the VR project

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The following list of publications (scientific journal articles, refereed conference proceedings, Theses, and technical reports) is structured by subprojects. Within each subproject, the publications are listed in alphabetical order by authors. Except for a few cases, the authors of a publication are listed alphabetically, which is the tradition we typically follow. Notice that several publications fit more than one subproject and are therefore listed under each of them.

### Square and Recursive Blocked Algorithms and Hybrid Data Structures

- [1] E. Elmroth, F. Gustavson, I. Jonsson, and B. Kågström. Recursive Blocked Algorithms and Hybrid Data Structures for Dense Matrix Library Software. *SIAM Review*, 46(1):3–45, 2004.
- [2] R. Granat, I. Jonsson, and B. Kågström. Recursive Blocked Algorithms for Solving Periodic Triangular Sylvester-Type Matrix Equations. In B. Kågström et al., editor, *Applied Parallel Computing: State of the Art in Scientific Computing, PARA 2006*, Lecture Notes in Computer Science, LNCS 4699, pages 531–539. Springer, 2007.
- [3] F. Gustavson, L. Karlsson, and B. Kågström. Distributed SBP Cholesky factorization algorithms with near-optimal scheduling. *ACM Trans. on Math. Software*, 36(2):11:1–11:25, March 2009. (Also published as Report UMINF 07.19 and IBM Research Report RC24342).
- [4] F. Gustavson, L. Karlsson, and B. Kågström. Three Algorithms for Cholesky Factorization on Distributed Memory Using Packed Storage. In B. Kågström et al., editor, *Applied Parallel Computing: State of the Art in Scientific Computing, PARA 2006*, Lecture Notes in Computer Science, LNCS 4699, pages 550–559. Springer, 2007.
- [5] I. Jonsson and B. Kågström. Recursive blocked algorithms for solving triangular systems. Part I. One-sided and coupled Sylvester-type matrix equations. *ACM Trans. Math. Software*, 28(4):392–415, 2002.
- [6] I. Jonsson and B. Kågström. Recursive blocked algorithms for solving triangular systems. Part II. Two-sided and generalized Sylvester and Lyapunov matrix equations. *ACM Trans. Math. Software*, 28(4):416–435, 2002.
- [7] Isak Jonsson. Recursive Blocked Algorithms, Data Structures, and High-Performance Software for Solving Linear Systems and Matrix Equations. *PhD Thesis* UMINF-03.17, Department of Computing Science, Umeå University, S-901 87 Umeå, Sweden, December, 2003.

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- [9] Lars Karlsson. *Blocked and Scalable Matrix Computations — Packed Cholesky, In-Place Transposition, and Two-Sided Transformations*. Ph. Licentiate Thesis, Dept. of Computing Science, Umeå University, Sweden, 2009. Report UMINF 09.11, ISBN 978–91–7264–788–6.
- [10] Lars Karlsson. Blocked in-place transposition with application to storage format conversion. Technical Report UMINF 09.01, Dept. of Computing Science, Umeå University, Sweden, 2009.

## Blocked and Parallel Matrix Equation Solvers

- [1] P. Andersson, R. Granat, and B. Kågström. Parallel Algorithms for Triangular Periodic Sylvester-type Matrix Equations. In E. Luque, T. Margalef, and D. Benítez, editors, *Euro-Par 2008 Parallel Processing – 14th International Euro-Par Conference*, volume LNCS 5168 of *Lecture Notes in Computer Science*, pages 780–789. Springer-Verlag, 2008.
- [2] R. Granat, I. Jonsson, and B. Kågström. Combining Explicit and Recursive Blocking for Solving Triangular Sylvester-Type Matrix Equations in Distributed Memory Platforms. In M. Danelutto, D. Laforenza, and M. Vanneschi, editors, *Euro-Par 2004*, volume 3149, pages 742–750. Lecture Notes in Computer Science, Springer, 2004.
- [3] R. Granat, I. Jonsson, and B. Kågström. RECSY and SCASY Library Software: Recursive Blocked and Parallel Algorithms for Sylvester-Type Matrix Equations with Some Applications. In R. Ciegis et al., editor, *Parallel Scientific Computing—Advances and Applications*, volume 27, pages 3–24. Springer Optimization and Its Applications, 2009.
- [4] R. Granat, I. Jonsson, and B. Kågström. Recursive Blocked Algorithms for Solving Periodic Triangular Sylvester-Type Matrix Equations. In B. Kågström et al., editor, *Applied Parallel Computing: State of the Art in Scientific Computing, PARA 2006*, Lecture Notes in Computer Science, LNCS 4699, pages 531–539. Springer, 2007.
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- [9] R. Granat, B. Kågström, and P. Poromaa. Parallel ScaLAPACK-style Algorithms for Solving Continuous-Time Sylvester Equations. In H. et al Kosch, editor, *Euro-Par 2003 Parallel Processing*, volume 2790, pages 800–809. Lecture Notes in Computer Science, Springer, 2003.

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- [11] Robert Granat. Algorithms and Library Software for Periodic and Parallel Eigenvalue Reordering and Sylvester-Type Matrix Equations with Condition Estimations. *PhD Thesis* UMINF-07.21, Department of Computing Science, Umeå University, S-901 87 Umeå, Sweden, November, 2007.
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- [18] SCASY - ScaLAPACK-style solvers for Sylvester-type matrix equations. See <http://www8.cs.umu.se/research/parallel/scasy>.

## Blocked and Parallel Two-Sided Reductions to Condensed Forms

- [1] B. Kågström, D. Kressner, E. Quintana-Orti, and G. Quintana-Orti. Blocked Algorithms for the Reduction to Hessenberg-Triangular Form Revisited. *BIT Numerical Mathematics*, 48(1):563–584, 2008.
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## Blocked and Parallel Reduction to Schur Forms

- [1] R. Granat, B. Kågström, and D. Kressner. A Novel Parallel QR Algorithm for Hybrid Distributed Memory HPC Systems. *SIAM J. Scientific Computing* (submitted), 2009. (Also as Lapack Working Note LAWN 216).

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- [5] D. Kressner. Block algorithms for reordering standard and generalized Schur forms. *ACM Trans. Math. Software*, 32(4):521–532, 2006.

## HPC Software and Tools

- [1] B. Adlerborn, B. Kågström, and D. Kressner. Parallel Variants of the Multishift QZ Algorithm with Advanced Deflation Techniques . In B. Kågström et al., editor, *Applied Parallel Computing: State of the Art in Scientific Computing, PARA 2006*, Lecture Notes in Computer Science, LNCS 4699, pages 117–126. Springer, 2007.
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- [10] SCASY - ScaLAPACK-style solvers for Sylvester-type matrix equations. See <http://www8.cs.umu.se/research/parallel/scasy>.

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